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Research Article

Influence of Humidity State on Dynamic Resilient Modulus of Subgrade Soils: Considering Repeated Wetting-Drying Cycles

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The service performance of subgrade depends on the dynamic resilient modulus (M_R) of subgrade soils. Meanwhile, due to complicated conditions such as rainfall infiltration, high temperature evaporation, and groundwater level fluctuations, it can be safely said that the humidity state and repeated wetting-drying (WD) cycles affect the M_R of subgrade soils. The object of this study is to conduct a series of dynamic triaxial tests after WD cycles to investigate the characteristics of the M_R under various factors. The main results are as follows: (i) the M_R decreased with the increase of deviator stress and rose with the growth of confining pressure; (ii) the humidification effect caused by the increase in moisture content attenuated the M_R ; (iii) the accumulation of WD cycles damaged the M_R ; however the decline rate was gradually retarded until it was stable with WD cycles 5 times; (iv) the satisfactory prediction model for the M_R of subgrade soils considering WD cycles was proposed and verified. It is expected that the findings can provide valuable contributions for road engineering.

1. Introduction

The dynamic resilient modulus (M_R) is a key parameter to characterize the stiffness characteristics of subgrade soils [1, 2], and it is employed as a basic input for determining the pavement structure thickness and combination method, for example, in the design standard of asphalt pavement in China (JTG D50-2017) and the guide of the American Association of State Highway and Transportation Officials (AASHTO 2002). Moreover, considering the stability and durability during the operation period, in addition to meeting stiffness requirements, the influence due to complex working environments on the service performance of road materials such as asphalt mixtures [3, 4], graded crushed rocks [5], and subgrade soils [6] is also a crucial issue that cannot be ignored. One of the universal occurrences is the change in the humidity of subgrade soils caused by a serious of reasons such as rainfall infiltration. According to longterm field tests data, the humidity of subgrade soils is not constant but gradually exceeds to the optimal moisture content (OMC) and eventually stabilized [7, 8]. The harmful wetting effect attenuates the M_R of subgrade soils with varying degrees, as many pavement diseases are attributed to this phenomenon, e.g., rutting [9], cracking [10], and bulge [11]. Therefore, it is of great significance to research the influence of humidity state on M_R of subgrade soils.

At present, researchers have carried out numerous studies on the influence of humidity changes on M_R of subgrade soils. Through two-year on-site monitoring, Elliott et al. [12] found that the actual moisture content of the subgrade soils progressively increased to 1.1 OMC. Subsequently, Zhang et al. [13] conducted soils humidity surveys on several expressways in southern China and reported that the moisture content of the subgrade soils continued to increase and finally stabilized at around 116% OMC. On this basis, they prepared high plasticity clays specimens under the moisture content conditions of 0.9 OMC, OMC, 1.1 OMC, 1.2 OMC, and 1.3 OMC, respectively, and performed corresponding repeated loading triaxial (RLT) tests [14]. The results showed that, under the given stress and compaction

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state, the increase in the moisture content of the specimen reduced the M_R . This rule was observed in the test results of Yao et al. [15] and Han et al. [16] for low liquid limit clays and seven different Canadian clays, respectively. For low liquid limit clays specimens with various moisture contents (OMC – 2%, OMC, and OMC + 2%) subjected to freezethaw cycles, Zhao et al. [17] claimed that whether it is a closed or open freezing method, the higher the moisture content, the lower the M_R , but the degree of attenuation is different. Zhang et al. [18] also used this level of moisture content to compact coarse grained fillers and organized RLT tests. The results captured the weakening effect of humidity growth on the M_R , in agreement with the findings on unbonded granular materials reported by Gu et al. [19] and recycled construction wastes reported by Azam et al. [20].

In addition to the experimental studies, the prediction model contributes to a better understanding of the M_R of subgrade soils. According to previous study, some representative models are available for M_R prediction. Hicks et al. [21] indicated that the stress level is the main factor affecting the M_R of materials and developed the k- θ model containing only the bulk stress, as shown in the following equation:

$$M_R = k_1 \theta^{k_2}, \tag{1}$$

where θ is the bulk stress, $\theta = \sigma_1 + \sigma_2 + \sigma_3$, σ_1 , σ_2 , and σ_3 are the major principal stress, the intermediate principal stress, and the confining pressure, respectively, and k_1 and k_2 are regression coefficients.

Lytton et al. [22] adopted the octahedral shear stress to characterize the shear effect, and the model was finally embodied in AASHTO 2002, as shown in the following equation:

$$M_R = k_1 P_a \left(\frac{\theta}{P_a}\right)^{k_2} \left(\frac{\tau_{\text{oct}}}{P_a} + 1\right)^{k_3},\tag{2}$$

where P_a = 101.3 kPa, which is the atmospheric pressure; τ_{oct} is the octahedral shear stress, $\tau_{oct} = (\sqrt{2}/3)\sigma_d$, $\sigma_d = \sigma_1 - \sigma_3$ is the deviator stress; k_3 is the regression coefficient.

Several scholars proposed that the influence of humidity state on the M_R should be directly reflected in the prediction model. Hence, the humidity parameter commonly employed in unsaturated soils mechanics, that is, the matric suction, was widely included in the prediction models. Liang et al. [23] believed the matric suction has the confinement impact, such as the bulk stress, so the matric suction and the bulk stress were combined into the same term, as shown in the following equation:

$$M_R = k_1 P_a \left(\frac{\theta + \chi \psi}{P_a}\right)^{k_2} \left(\frac{\tau_{\text{oct}}}{P_a} + 1\right)^{k_3},\tag{3}$$

where χ is the effective stress parameter ($\chi \in [0,1]$, determined by the properties of different materials); ψ is the matric suction, $\psi = u_a - u_w$, u_a is the pore-air pressure, and u_w is the pore-water pressure.

Given that the bulk stress could not separate the constraint effect and shear effect because the bulk stress contains

the confining stress and maximum cyclic stress, Yao et al. [15] defined the minimum bulk stress θ_m and built

$$M_R = k_1 P_a \left(\frac{\psi}{P_a} + 1\right)^{k_2} \left(\frac{\theta_m}{P_a}\right)^{k_3} \left(\frac{\tau_{\text{oct}}}{P_a} + 1\right)^{k_4},$$
 (4)

where $\theta_m = \sigma_1 + \sigma_2 + \sigma_3 - \sigma_d = 3\sigma_3$ is the minimum bulk stress; k_4 is the regression coefficient.

Zhang et al. [18], based on the laws obtained from the RLT tests of construction and demolition wastes, established the model that can consider the number of freeze-thaw cycles, compactness, humidity state, and stress state as shown in the following equation:

$$M_{R} = k_{1} P_{a} \left[\ln \left(N + e \right) \right]^{k_{2}} C^{k_{3}} \left(\frac{\psi}{P_{a}} + 1 \right)^{k_{4}} \left(\frac{\theta_{m}}{P_{a}} \right)^{k_{5}} \left(\frac{\tau_{\text{oct}}}{P_{a}} + 1 \right)^{k_{6}}, \tag{5}$$

where N is the number of freeze-thaw cycles; C is the compactness; and k_5 and k_6 are regression coefficients.

In general, the related studies provided insightful and constructive comments into the influence of humidity state on M_R of subgrade soils. However, to the best of the authors' knowledge, due to rainwater infiltration and lateral migration, and transpiration during high temperature periods, the humidity of subgrade soils is not increasing continuously but undergoes intricate wetting and drying processes and finally reaches an equilibrium state. Therefore, the specimens were directly prepared with the final equilibrium moisture content and the tests conducted failed to accurately fit the actual humidity change process of the subgrade soils. Also, limited by the cumbersome and time-consuming test process [24, 25], it is inconvenient to use the matric suction as the humidity parameter. Furthermore, there are few reports on the prediction model of M_R considering the repeated wetting-drying (WD) cycles.

To address the above problems, the subgrade soils were investigated through a series of WD cycles tests and RLT tests. From the experimental results, the influences of stress state, humidity state, and WD cycles on the M_R were analyzed. On this basis, the prediction model of the M_R that can consider repeated WD cycles was established and verified. The main findings of this study were summarized in the last section, which can supply novel contributions and technical supports to the theory for pavement design.

2. Experiments Approach

2.1. Materials and Specimens. The studied soils in this study were from Changsha City, Hunan Province, China. The particle size analysis is listed in Figure 1. The standard heavy compaction tests were conducted to acquire the OMC and maximum dry density of the soils. In accordance with the Chinese Guidance for Test Methods of Soils on Highway Engineering, other main basic physical properties had also been determined in Table 1. Based on these parameters, the soils were named as high liquid limit silts (MH) according to the Unified Soils Classification System.

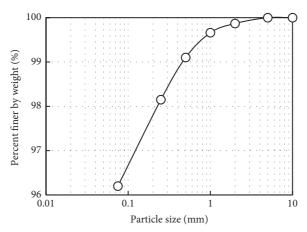


FIGURE 1: Distribution curves of particle size.

TABLE 1: Basic physical properties of the used soils.

Liquid limit (%)	Plastic limit (%)	Plastic index	Maximum dry density	Optimum moisture content (%)	Specific gravity
51.7	37.1	14.6	$1.62\mathrm{g/cm}^3$	22.6	2.71

To ensure consistent compactness and humidity levels between specimens, all the soils were prepared in the laboratory. Firstly, the soils were crushed and collected after filtering by the 5 mm sieve and then dried at 105°C for 12 h. Subsequently, the dry soils were mixed with distilled water under the OMC in order to simulate the initial humidity state of soils during subgrades filling [26] and then stored in a sealed plastic bag for 24 h so that the moisture was uniform. Meanwhile, the compactness of the specimens was set to 96% based on China's current requirements for road beds. Afterwards, the wet soils with the calculated mass were compacted by five layers into a cylinder that was 100 mm in diameter and 200 mm in height. Finally, the specimens were wrapped to avoid water evaporation.

2.2. Wetting-Drying Cycles. At present, the common practice to achieve WD cycles is to soak the specimens in water to the target wet side moisture content and then place them in the oven to dry at high temperature to the target dry side moisture content [27, 28]. Although this pattern speeds up the test process, the water absorption and dehydration of the specimens are obviously much faster than the actual water exchange rate of subgrade soils. To this end, this study applied a novel method as shown in Figure 2; that is, the specimens were set in the diffuse misty air generated by the atomizer to absorb water and add humidity by capillary action. After the moisture content of the specimens reached the target value, they were transferred to an oven with an internal temperature of 50°C for drying. Such a way is more suitable for depicting the wetting and drying condition of soils on site.

Given the possible variation range of the equilibrium humidity state of the subgrade soils, the final actual moisture contents of specimens were set to 0.9 OMC, OMC, 1.1 OMC, 1.2 OMC, and 1.3 OMC, respectively. The specimens prepared under OMC were first humidified to 1.3 OMC and then dehumidified to 0.9 OMC. The two parts were regarded

as one WD cycle, and then so on. The numbers of WD cycles in this study were designed as 0, 1, 3, and 5. After the specimens have experienced the preset WD cycles, they changed from 0.9 OMC to the anticipant target moisture content. Taking the WD cycles 3 times and the final actual moisture content of 1.2 OMC as an example, the humidity change path is as follows: OMC \longrightarrow 1.3 OMC \longrightarrow 0.9 $OMC \longrightarrow 1.3 \quad OMC \longrightarrow 0.9 \quad OMC \longrightarrow 1.3 \quad OMC \longrightarrow 0.9$ $OMC \longrightarrow 1.2 OMC \longrightarrow wrapped$ and allowed to stand for 1-2 days \longrightarrow RLT tests. In order to determine the key nodes when the humidification moisture content (w_n) and the dehumidification moisture content (w_D) of the specimens reached the target level, it is necessary to grasp the humidity change rate. In this study, the specimens were weighed every about 10 h, and the results are summarized in Figure 3. Based on this finding, the moment when the humidity of the specimen reached the target value can be estimated, namely, the weighing frequency can be increased for some time before this moment to control the required moisture content of the specimen.

2.3. Repeated Loading Triaxial Tests. DYNATRIAX-100/14, the dynamic triaxial test equipment, was used to measure the M_R of specimens in this study. The load form adopted halfsine wave, the frequency was 1 Hz, the action time was 0.2 s, and the intermittent time was 0.8 s. The stress conditions referred to the RLT sequence for subgrade fine-grained soils proposed by Luo [29], as shown in Table 2, benefiting from its comprehensive coverage of the stress range of the subgrade work area in China. In this sequence, the deviator stresses were designed as four groups from low to high, and the confining pressures in each group were divided into four levels from great to small so as to reduce the possibility of premature failure of the specimens during the loading process. The test data of the last five cycles in each stress combination are to acquire the corresponding M_R value.

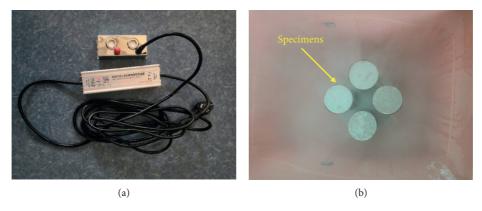


FIGURE 2: The atomization and humidification process of the specimens. (a) Atomizer. (b) Humidification.

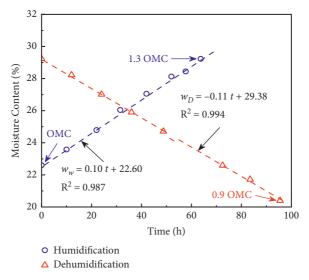


Figure 3: The relationship between \boldsymbol{w}_{w} and \boldsymbol{w}_{D} and time (t), respectively.

TABLE 2: The stress-loading sequence in this study.

No.	Confining pressure σ_3 (kPa)	Contact pressure 0.2 σ_3 (kPa)	Deviator stress σ_d (kPa)	Principal stress ratio σ_{I}/σ_3	Number of cycles
0 (preloading)	30	6	55	2.8	2000
1	60	12	30	1.5	100
2	40	9	30	1.8	100
3	30	6	30	2.0	100
4	15	3	30	3.0	100
5	60	12	55	1.9	100
6	40	9	55	2.4	100
7	30	6	55	2.8	100
8	15	3	55	4.7	100
9	60	12	75	2.3	100
10	40	9	75	2.9	100
11	30	6	75	3.5	100
12	15	3	75	6.0	100
13	60	12	105	2.8	100
14	40	9	105	3.6	100
15	30	6	105	4.5	100
16	15	3	105	8.0	100

3. Analysis of Influence Factors of the Dynamic Resilient Modulus

3.1. Influence of Deviator Stress on the Dynamic Resilient *Modulus.* Figure 4 shows the variation of M_R with deviator stress under different confining pressures and moisture content before WD cycles. It can be observed that M_R decreases with the enhancement of deviator stress. The possible principle behind this phenomenon is that the growth of the deviator stress leads to an increase in the vertical strain, and the increase of the vertical strain is greater than the increase of the deviator stress, which ultimately leads to a decrease in M_R . Taking the event of confining pressure of 30 kPa and moisture content of 1.1 OMC as an example, when the deviator stress rises from 30 kPa to 55 kPa, 75 kPa, and $105 \,\mathrm{kPa}$, M_R attenuates by 12.03%, 14.18%, and 30.55%, respectively. Obviously, the soils specimens presented softening behavior, which is consistent with the previous findings of many researchers [14, 15]. It is worth pointing out that because $\tau_{\text{oct}} = (\sqrt{2}/3)\sigma_d$, the octahedral shear stress and deviator stress have the same influence rule on the M_R .

3.2. Influence of Confining Pressure on the Dynamic Resilient *Modulus.* Figure 5 reveals the nonlinear positive correlation between M_R and the confining pressure with various moisture content and deviator stress at WD cycle 1 time. For instance, under the deviator stress of 75 kPa and the moisture content of 0.9 OMC, as the confining pressure gradually increases from 15 kPa to 30 kPa, 40 kPa, and $60 \,\mathrm{kPa}$, M_R value expands 19.74%, 28.95%, and 43.42% respectively. It can be seen that the confining pressure has a considerable lateral restraint effect on the specimens, so that it has a better stiffness holding capacity to resist vertical deformation under a higher deviator stress, in agreement with the results obtained in the past few decades [14, 16, 30]. Similarly, according to the equivalence relationship $\theta_m = 3\sigma_3$, the minimum bulk stress and confining pressure also have the coincident influence on the M_R .

3.3. Influence of Moisture Content on the Dynamic Resilient Modulus. Figure 6 illustrates that, under the given stress states, the humidification effect significantly reduces the M_R of the specimens. For example, for the case of WD cycles 5 times and the confining pressure of 40 kPa, as the moisture content increases from 0.9 OMC to 1.3 OMC, the attenuation range of M_R with various deviator stresses is 43.02%-67.35%. It shows that the increased humidity causes the specimens to soften. The possible explanation is that water has a certain lubricating effect among soils particles. When the moisture content decreases, the water film on the surface of the soils particles is thinner, and the relative movement between the soils particles is more difficult, so the specimens have a stronger ability to resist deformation. Conversely, the increase in moisture content makes the relative movement between soils particles simpler, and the specimens are less resistant to deformation; namely, the stiffness is reduced.

3.4. Influence of Wetting-Drying Cycles on the Dynamic Resilient Modulus. In order to intuitively reflect the impact of repeated WD cycles on the M_R , referring to the way that Zhang et al. [18] defined the freeze-thaw damage factor, this study employed the WD damage factor as the evaluation indicator, as shown in the following equation:

$$D = \frac{M_{R(0)} - M_{R(i)}}{M_{R(0)}},\tag{6}$$

where D is the WD damage factor; $M_{R(0)}$ is M_R before WD cycles; $M_{R(i)}$ is M_R after the i times WD cycles, and i = 0, 1, 3, 5 here

Figure 7 indicates that, under the given moisture content and stress state, the damage factor increases with the accumulation of WD cycles. In particular, the attenuation of M_R is the most obvious by the first WD effect, and the damage factor ranges from 0.27 to 0.54. With the increase of the numbers of WD cycles, the growth rate of the damage factor gradually slows down and finally basically stabilizes. At the same time, the damage factor of M_R after WD cycles 5 times is 0.63 to 0.95. Compared with the 3th cycle of WD cycles, the increase of the damage factor is less than 10%. It can be considered that the stiffness of the specimen is stable after 5 WD cycles.

Annotation: (60 kPa, 30 kPa) denotes that the confining pressure is 60 kPa, and the deviator stress is 30 kPa. For clarity, only partial test results under various stress states are given.

4. Prediction Model for the Dynamic Resilient Modulus with Wetting-Drying Cycles

This section aims to establish a phenomenological model of the M_R that can consider the WD cycles. A satisfactory prediction model should comprehensively include influencing factors and reasonably reflect the influence law of each factor on M_R [31]. Based on the analysis in the previous section, the numbers of WD cycles, actual moisture content, minimum bulk stress, and octahedral shear stress are selected as independent variables. In particular, the actual moisture content is used instead of matric suction to characterize the humidity state, and the rewritten exponential form is applied to reflect the WD cycles impact, the established model as shown in (7). A total of $4 \times 5 \times 16$ (the numbers of WD cycles × the actual moisture content levels × the stress states) = 320 sets of tests data in this study were used to fit the model, and the results were summarized in Table 3.

$$M_R = k_1 P_a e^{k_2 N} \left(\frac{w}{\text{OMC}}\right)^{k_3} \left(\frac{\theta_m}{P_a}\right)^{k_4} \left(\frac{\tau_{\text{oct}}}{P_a} + 1\right)^{k_5},$$
 (7)

where N is the numbers of WD cycles; w is the actual moisture content; $k_1 \sim k_5$ are the model parameters, and other symbols have the same meaning as above.

For the fit result, k_1 is the coefficient which must be a positive number because M_R cannot be negative. k_2 as an exponent must be a negative number, because with the growth of the number of WD cycles, M_R reduces. k_3 should

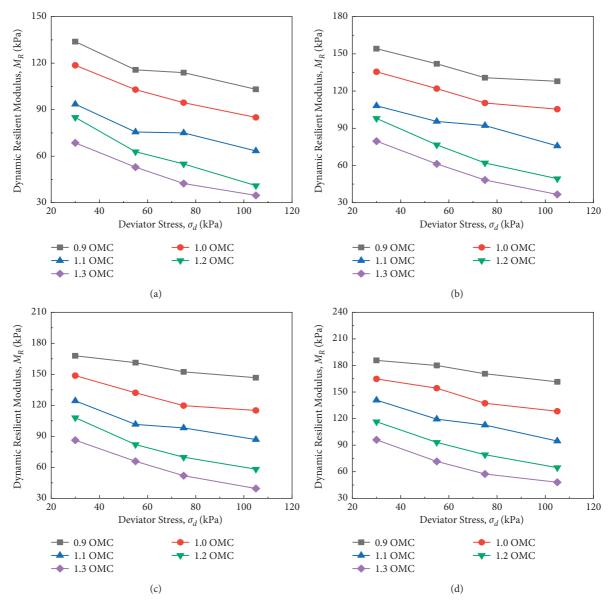


FIGURE 4: The relationship between σ_d , moisture content, and M_R at WD cycles = 0. (a) $\sigma 3 = 15$ kPa. (b) $\sigma 3 = 30$ kPa. (c) $\sigma 3 = 40$ kPa. (d) $\sigma 3 = 60$ kPa.

be a negative number, on account of the higher the actual moisture content, the smaller the M_R . According to the restraint effect caused by the minimum bulk stress and the softening effect produced by the octahedral shear stress on the soils specimens, it can be inferred that $k_4 > 0$ and $k_5 < 0$. Obviously, the results shown in Table 3 are consistent with the analysis of the experimental rules in this study. In addition, the value of the determination coefficient R^2 exceeds 0.9, indicating that the prediction model exhibited in (7) is excellent. In order to have confidence in this model, this study is done in conjunction with relevant experimental data

from other researchers to verify (7) [32], and the results are shown in Figure 8. It can be seen that the measured M_R is close to the predicted value. Although R^2 is slightly lowered, this may be due to the difference in the actual process of the specimens being subjected to WD cycles, which leads to a decrease in the accuracy of (7), but the prediction effect is still excellent based on the recommended criteria for evaluating R^2 in road engineering [33–35]. Therefore, it can be speculated that this model is applicable to other soils although it is only proposed based on the high liquid limit silts taken from Changsha City, China, in this study.

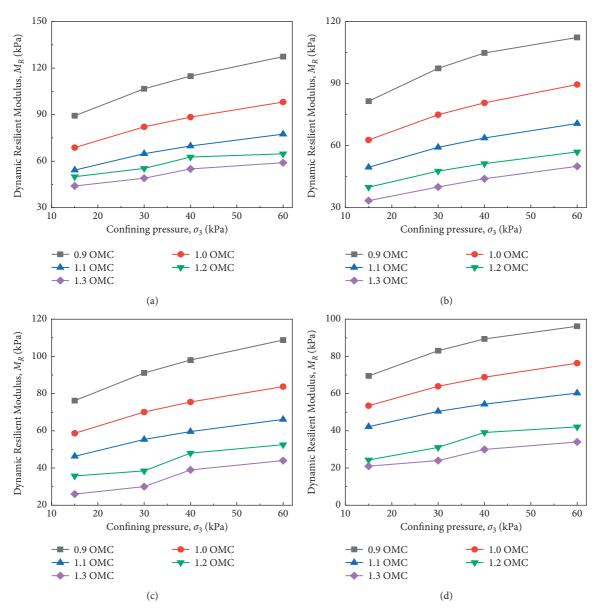


FIGURE 5: The relationship between σ_3 , moisture content, and M_R at WD cycles = 1. (a) σ_d = 30 kPa. (b) σ_d = 55 kPa. (c) σ_d = 75 kPa. (d) σ_d = 105 kPa.

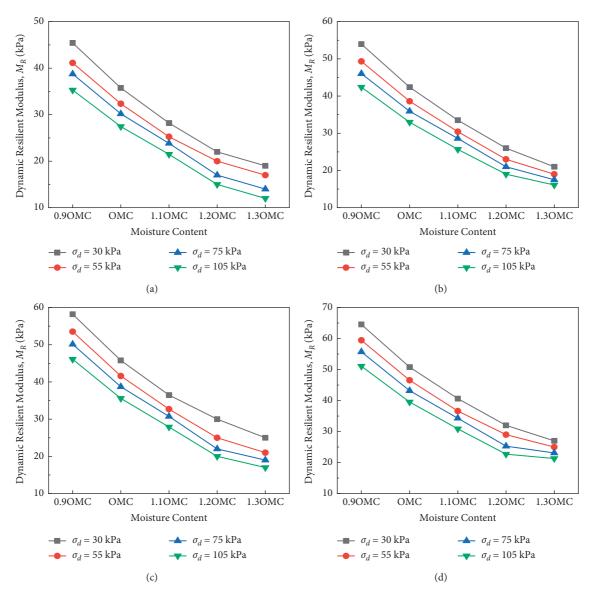


FIGURE 6: The relationship between σ_d , moisture content, and M_R at WD cycles = 5. (a) $\sigma_3 = 15$ kPa. (b) $\sigma_3 = 30$ kPa. (c) $\sigma_3 = 40$ kPa. (d) $\sigma_3 = 60$ kPa.

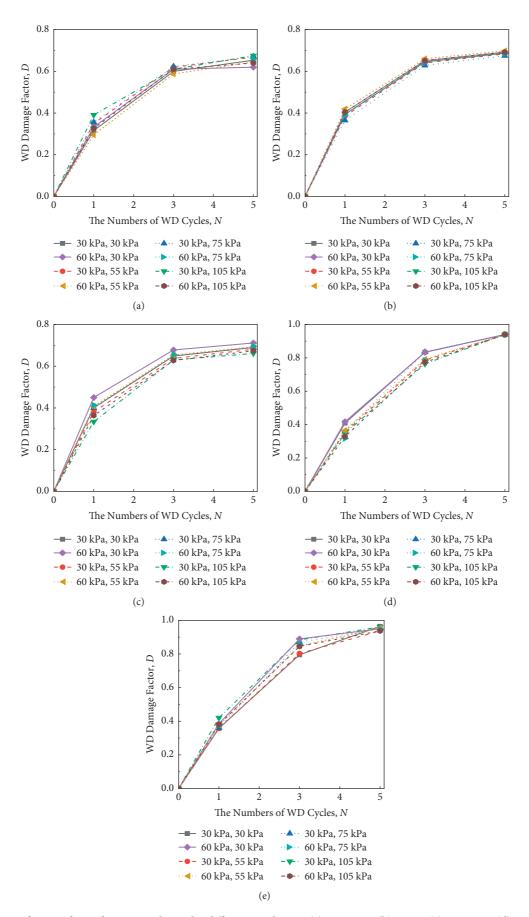


FIGURE 7: Damage factors of M_R after WD cycles under different conditions. (a) 0.9 OMC. (b) OMC. (c) 1.1 OMC. (d) 1.2 OMC. (e) 1.3 OMC.

TABLE 3: The fitting results of equation (7) in this study.

k_1	k_2	k_3	k_4	k_5	R^2
1.49	-0.29	-2.35	0.28	-1.13	0.94

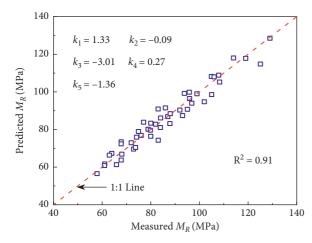


Figure 8: The predicted by equation (7) and measured M_R in another studies.

5. Conclusions

This study aimed at revealing the influence of humidity state on M_R of subgrade soils considering WD cycles. For this purpose, this study carried out a series of WD cycles and RLT tests. Based on the analysis of experimental results, the main findings of this research can be summarized as follows:

- (1) The innovative humidification method was realized by using atomizer, which was more consistent with the actual WD cycles condition of subgrade soils. According to the exploratory tests, the change relationship between moisture content and time in the process of humidification and dehumidification of the specimens was mastered, so as to provide technical support for accurately controlling the key nodes of WD cycles.
- (2) The stress state has a significant effect on the stiffness of subgrade soils; that is, M_R decreased with the increase of deviator stress and increased with the rise of confining pressure. Meanwhile, the humidification due to the growth in moisture content led to a decrease in M_R. In addition, the accumulation of repeated WD cycles attenuated M_R, but the decay rate gradually slowed down until it stabilized after 5 WD cycles.
- (3) This study employed the ratio of actual moisture content to OMC to characterize the humidity state, the improved exponential form reflected the influence of WD cycles, and the minimum bulk stress and octahedral shear stress embodied the constraint and shear effect, respectively. On this basis, a novel and excellent prediction model for M_R of subgrade soils was established.

It is worth emphasizing that although the applicability of the proposed model to the data of other researchers is successful, the focus in the future should continue to search for more soils tests data for verification to ensure the robustness of the model.

Data Availability

Some or all data and models that support the findings of this study are available from the corresponding author upon reasonable request.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

Acknowledgments

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