

Half-mass Radii of Quiescent and Star-forming Galaxies Evolve Slowly from $0 \leq z \leq 2.5$: Implications for Galaxy Assembly Histories^{*}

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Abstract

We use high-resolution, multiband imaging of ~16,500 galaxies in the CANDELS fields at $0 \le z \le 2.5$ to study the evolution of color gradients and half-mass radii over cosmic time. We find that galaxy color gradients at fixed mass evolve rapidly between $z \sim 2.5$ and $z \sim 1$, but remain roughly constant below $z \sim 1$. This result implies that the sizes of both star-forming and quiescent galaxies increase much more slowly than previous studies found using half-light radii. The half-mass radius evolution of quiescent galaxies is fully consistent with a model that uses observed minor merger rates to predict the increase in sizes due to the accretion of small galaxies. Progenitor bias may still contribute to the growth of quiescent galaxies, particularly if we assume a slower timescale for the minor merger growth model. The slower half-mass radius evolution of star-forming galaxies is in tension with cosmological simulations and semianalytic galaxy models. Further detailed, consistent comparisons with simulations are required to place these results in context.

Unified Astronomy Thesaurus concepts: Galaxy evolution (594); Galaxy formation (595); Galaxy radii (617); Galaxy structure (622)

1. Introduction

Examining how star-forming and quiescent galaxies grow in size over cosmic time can provide clues about galaxy evolution. In combination with other measured properties, sizes inform studies of the mass assembly history of galaxies (e.g., Bezanson et al. 2009; Naab et al. 2009), the connections between galaxies and their host dark matter halos (e.g., Mo et al. 1998; Kravtsov 2013; Somerville et al. 2018; Jiang et al. 2019), how galaxy populations change (e.g., Carollo et al. 2013; Poggianti et al. 2013) and disks build up over time (e.g., van Dokkum et al. 2013).

Star-forming galaxies seem to grow more slowly than zeroth-order expectations for dark matter halo growth (Mo et al. 1998), perhaps due to evolving halo spin parameters (e.g., Somerville et al. 2008) or feedback processes (e.g., Dutton & van den Bosch 2009). Recent abundance matching studies including this additional physics have found that the observed sizes of disky star-forming galaxies are indeed proportional to the virial radii of their host halos (e.g., Kravtsov 2013; Huang et al. 2017; Somerville et al. 2018). Cosmological simulations have also found good agreement between observed and modeled star-forming galaxy size evolution (Furlong et al. 2017; Genel et al. 2018).

Quiescent galaxies appear to grow in size incredibly rapidly, especially at high redshift (e.g., Daddi et al. 2005; van Dokkum et al. 2008; Damjanov et al. 2009, 2011; Szomoru et al. 2010; van der Wel et al. 2014). Two theories have arisen to explain this rapid size evolution: in the "inside-out growth" scenario, individual quiescent galaxies grow via minor mergers (e.g., Bezanson et al. 2009; Hopkins et al. 2009; Naab et al. 2009; van de Sande et al. 2013); in the "progenitor bias" scenario, the

median size of the quiescent population increases with time because galaxies that quench at later times are larger (e.g., van Dokkum & Franx 2001; Carollo et al. 2013; Poggianti et al. 2013). The apparent size growth of quiescent galaxies could be explained by individual growth, population growth, or a combination of both processes.

All of these observational studies measure galaxy sizes from stellar light profiles. However, radial M/L variations cause a galaxy's light profile to differ from its mass profile. Therefore, half-light radii are *biased tracers* of galaxy mass distributions if M/L gradients are present. In Suess et al. (2019), we measured the half-mass radii of ~7000 galaxies from multiband high-resolution imaging and showed that the strength of color gradients in both star-forming and quiescent galaxies evolves between z = 1.0 and z = 2.5. As a result, the evolution of galaxy half-mass radii differs from the previously reported half-light radius evolution. In this Letter, we extend our previous analysis to lower redshifts. Using this uniform sample of half-mass radii from $0 \leq z \leq 2.5$, we analyze and discuss how star-forming and quiescent galaxies grow in size over cosmic time.

Throughout this Letter, we assume a cosmology of $\Omega_{\rm m} = 0.3$, $\Omega_{\Lambda} = 0.7$, and h = 0.7; all radii are noncircularized measurements of the major axis.

2. Sample, Methods, and Galaxy Half-mass Radii

In this Letter, we present the evolution of galaxy half-mass radii from z = 2.5 to $z \sim 0$. From $1.0 \le z \le 2.5$, we use the sample of galaxy half-mass radii presented in Suess et al. (2019). This high-redshift sample consists of 7006 galaxies selected from the ZFOURGE photometric catalog (Straatman et al. 2016) to have $\log M_*/M_{\odot} > 9.0$, $S/N_K \ge 10$, a use flag equal to one, a match in the 3D-HST catalog (Brammer et al. 2012; Skelton et al. 2014; Momcheva et al. 2016), and a convergent GALFIT fit (Peng et al. 2002; van der Wel et al. 2014).

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Here, we expand our previous work by presenting the halfmass radii of an additional 9543 galaxies at $z \leq 1.0$. This lowredshift sample consists of all galaxies in the 3D-HST photometric catalog with $z \leq 1.0$, $\log M_*/M_{\odot} > 9.0$, $S/N_{F160W} \ge 10$, a use flag equal to one, and a convergent GALFIT fit. These selection criteria are equivalent to those of the higher-redshift sample presented in Suess et al. (2019), but using the 3D-HST catalogs as opposed to the ZFOURGE catalogs. This allows us to include galaxies from the AEGIS and GOODS-N fields (not included in ZFOURGE) and better sample the $z \leq 0.5$ universe. Furthermore, we note that recovered galaxy properties at z < 1 do not change significantly with the inclusion of the ZFOURGE data: at these low redshifts, the medium-band filters in ZFOURGE no longer sample the Balmer break.

We calculate the half-mass radii of galaxies in the lowredshift sample following the methods of Suess et al. (2019). In brief: we calculate aperture photometry in elliptical annuli for each galaxy in each band of point-spread function-convolved HST imaging (Skelton et al. 2014), then use FAST (Kriek et al. 2009) to model the resulting spatially resolved spectral energy distributions (SEDs). This method produces an as-observed M/L profile for each galaxy. We correct for the effects of the point-spread function with a simple forward modeling technique which assumes that that the intrinsic M/L profile is a power-law function of radius. We then use the best-fit intrinsic M/L profile in conjunction with the galaxy's light profile and the point-spread function to find the half-mass radius. Full details of this method and comparisons with other techniques for measuring half-mass radii are presented in Suess et al. (2019). Suess et al. (2019) also show that the half-mass radii recovered using our technique are not significantly biased by the galaxy's half-light radius, stellar mass, or redshift.

In Figure 1, we show the strength of galaxy color gradients (i.e., $r_{e,mass}/r_{e,light}$) as a function of stellar mass for two redshift slices in our new low-redshift sample. We divide the sample into star-forming and quiescent populations using the UVJ diagram and the quiescent definition from Whitaker et al. (2012). In Suess et al. (2019), we found that there was a significant trend between color gradient strength and stellar mass for galaxies at $1.0 \le z \le 2.5$. Here, we find that this trend continues to lower redshifts. The only exception is in the lowest-redshift quiescent bin, where our sample is quite small. In the lower panels of Figure 1, we also show how the best-fit relation between $r_{e,mass}/r_{e,light}$ and stellar mass varies as a function of redshift for our full $0 \le z \le 2.5$ sample.

In Figure 2, we show the median strength of color gradients for all galaxies with $\log M_*/M_{\odot} > 10.1$, the completeness limit of our full sample. In Suess et al. (2019), we showed that the strength of galaxy color gradients decreases sharply between $z \sim 2.5$ and $z \sim 1$. Here we find that this evolution may flatten below $z \sim 1$; $r_{e,mass}/r_{e,light}$ for both quiescent and star-forming galaxies remains roughly constant at a value of ~0.7.

3. The Growth of Quiescent Galaxies Is Consistent with Minor Merger Predictions

Over the past decade, numerous studies have assessed how merger-driven inside-out growth and progenitor bias can contribute to the size evolution of quiescent galaxies (e.g., Bezanson et al. 2009; Hopkins et al. 2009; Carollo et al. 2013; Poggianti et al. 2013; van de Sande et al. 2013; Williams et al. 2017; Damjanov et al. 2019). Several studies—notably

Newman et al. (2012) and Belli et al. (2015)—attempt to tease out the relative contributions of these two growth mechanisms. Newman et al. (2012) studied the merger rates of galaxies in the CANDELS survey and calculated the resulting effect on galaxy sizes. They found that while minor mergers could explain the relatively slow growth in half-light radii at $z \sim 1$, minor mergers were *insufficient* to explain the much more rapid growth at $z \sim 2$. In a similar vein, Belli et al. (2015) infer the star formation histories of quiescent galaxies and reconstruct the size evolution of the quiescent population. They find that both individual growth and progenitor bias must contribute (in roughly equal proportions) to the observed increase in the halflight radii of quiescent galaxies. Both individual and population growth seem to be necessary to explain the increase in quiescent galaxy sizes, especially at early times when half-light radii grow very rapidly. However, both of these studies used half-light radii to study quiescent size growth; here, we use half-mass radii to account for the bias due to evolving color gradients.

In Figure 3, we show the evolution of the half-light and halfmass radii of quiescent galaxies at $M_* = 10^{10.7} M_{\odot}$. The gray curve shows the half-light radius evolution, with data taken from Mowla et al. (2019). The black curve shows the evolution of quiescent half-mass radii at the same stellar mass. The halfmass radius data points are calculated by multiplying our bestfit relation for $r_{\rm e,mass}/r_{\rm e,light}-M_*$ (Figure 1) by the Mowla et al. (2019) $r_{\rm e,light}-M_*$ relations, as described in more detail in Suess et al. (2019). While the half-mass and half-light radii of massive quiescent galaxies are nearly equal at z = 2.25, halfmass radii grow much less rapidly than half-light radii do.

We compare this size evolution to the Newman et al. (2012) predictions for quiescent galaxy growth via minor mergers. Like Newman et al. (2012), we assume a merger timescale $\tau_e = 1.0 \,\text{Gyr}$. The shaded red region in Figure 3 shows this model; the width represents the measured uncertainty in the merger fraction. Between z = 2.25 and z = 1, this data-based model predicts that minor mergers cause galaxy sizes to grow by (0.12 ± 0.04) dex. As identified by previous works, minor mergers alone cannot explain the 0.28 dex increase in galaxy half-light radii found over the same redshift range. However, the growth in half-mass radii (which we measure to be 0.14 dex) is fully consistent with a model that includes minor mergers alone. No additional mechanism for size growth at high redshift is necessary to explain the observed half-mass radius evolution. Between z = 0.75 and z = 0.4, the Newman et al. (2012) model predicts a size increase of (0.10 ± 0.04) dex due to minor mergers. Observed half-light radii grow by 0.10 dex, and observed half-mass radii grow by 0.14 dex; both are consistent with the data-based merger growth model. As discussed in Suess et al. (2019), our observed color gradient evolution at high redshift also supports an inside-out growth or two-phase formation scenario (Naab et al. 2009; Oser et al. 2010): minor mergers deposit bluer stars at the outskirts of the galaxy, creating negative color gradients. As redshift decreases and galaxies experience more minor mergers, these color gradients become stronger.

We note that in Figure 3 we invoke a fast merger timescale of $\tau_e = 1.0$ Gyr. A slower merger timescale would decrease the amount of size growth that minor mergers can account for. In this case, there would still be additional growth in quiescent half-mass radii that must be accounted for by progenitor growth. A careful study of the half-mass radii of the smallest



Figure 1. Top: color gradient strength as a function of stellar mass for two redshift intervals. Small light blue points and light red squares show individual star-forming and quiescent galaxies; large blue points and red squares show a running median. The blue and red lines show best-fit linear relations to each trend; lines are outlined in black if the slope of the relation is inconsistent with zero, and outlined in gray if the slope is consistent with zero. Dashed vertical blue and red lines show the mass completeness of the star-forming and quiescent samples. Bottom: best-fit relation between color gradient strength and stellar mass for star-forming (left) and quiescent (right) galaxies as a function of redshift. Dashed lines represent fits whose slopes are consistent with zero. We see clear redshift evolution in the best-fit color gradient-mass relations for both quiescent and star-forming galaxies.

quiescent galaxies over time (e.g., Carollo et al. 2013), potentially in combination with stellar abundance studies (e.g., Kriek et al. 2016, 2019), is required to fully understand how much progenitor bias contributes to quiescent half-mass radius growth.

4. The Slow Growth of Star-forming Galaxies Is Inconsistent with Simulations

We now examine the growth of star-forming galaxies when including the effects of color gradients. Figure 4 shows how the half-light and half-mass radii of star-forming galaxies evolve. The overall picture is similar to that of quiescent galaxies: starforming galaxies have roughly equal half-mass and half-light radii at early times; however, half-mass radii evolve much more slowly than half-light radii. This shallow size evolution is supported by spatially resolved spectral studies: low- and intermediate-mass star-forming galaxies at $z \sim 2$ have nearly flat sSFR profiles, implying self-similar growth and thus slow size evolution (Tacchella et al. 2015a, 2015b; Nelson et al. 2016).

Many cosmological simulations and semianalytic models predict the size evolution of star-forming galaxies based on their mass distributions. Interestingly, the evolution of these simulated half-mass radii generally matches the observed half-light radius evolution, not the slower half-mass radius evolution we show in Figure 4. Hence, the simulations predict a much stronger evolution in star-forming half-mass radii than our observations. For example, Furlong et al. (2017) show that the predicted half-mass radii of disk galaxies in the EAGLE simulations are consistent with observed half-light radii within ≤ 0.1 dex; their modeled half-mass radii show a similar redshift



Figure 2. Median half-mass to half-light radius ratio for star-forming and quiescent galaxies (blue circles and red squares) as a function of redshift. $r_{\text{mass}}/r_{\text{light}}$ traces the strength of radial color gradients; values less than one indicate negative color gradients, where the center of the galaxy is redder than the outskirts. Only galaxies with $\log M_*/M_{\odot} > 10.1$, where our sample is complete, are included. Error bars show the central 68% of 500 bootstrap samples. The strong color gradient evolution previously observed at $z \gtrsim 1$ appears to flatten at $z \lesssim 1$.

evolution as the van der Wel et al. (2014) half-light radius observations. The half-mass radii of galaxies in Illustris-TNG also evolve at a similar rate as observed half-light radii (Genel et al. 2018). The semianalytic model of Dutton et al. (2011) predicts the evolution of disk sizes as well as the strength of color gradients in disk galaxies; their half-mass radius evolution is generally consistent with observations of half-light radii, not with our observed half-mass radii.

Several physical processes could account for this discrepancy between simulated and observed half-mass radii. Dutton & van den Bosch (2009) found that including feedback in semianalytic models slows down the expected size evolution of disk galaxies. If the effects of feedback were slightly stronger —or the physics of feedback was slightly different—it may be possible to further slow the modeled evolution of star-forming half-mass radii and bring them in line with our observations. Higher merger rates at high redshift could also weaken the evolution of simulated disk sizes. Additional explanations for this discrepancy—which could apply to measurements of halfmass radii for both star-forming and quiescent galaxies—are discussed in more detail below.

5. Discussion

In general, most modern simulations predict both the mass distributions and the light distributions of model galaxies, then report half-light radii which can be directly compared to observations. The measured half-light radius evolution of both star-forming and quiescent galaxies from these simulations is in good agreement with observations: the half-light radii typically agree to within 0.1–0.25 dex (Somerville et al. 2008; Dutton et al. 2011; Price et al. 2017; Genel et al. 2018). This is particularly interesting in light of our results: first, if the



Figure 3. Half-light radius (open gray points) and half-mass radius (filled black points) of quiescent galaxies at $10^{10.7} M_{\odot}$ as a function of lookback time. Red shaded regions show the expected growth via minor mergers using the Newman et al. (2012) models, assuming a merger timescale of $\tau_e = 1.0$ Gyr. Minor mergers alone are sufficient to explain the growth of half-mass radii.

modeled half-light radii agree with observations while the modeled half-mass radii do not (Section 4), then both the halfmass radii and the color gradients in the simulations may differ from what we observe; second, because these simulations already include color gradients, these simulated color gradients can now be directly compared with our new color gradient measurements.

To date, very few studies have discussed color gradients in simulated galaxies. Dutton et al. (2011) used a semianalytic model of disks evolving within dark matter halos to compare observed and simulated galaxy scaling relations. They report both half-mass radii and half-light radii in several different filters. Color gradients in their simulated galaxies seem to evolve less rapidly than our observations, decreasing by only ~ 0.1 dex between z = 2.5 and z = 0.25; over the same redshift range, our measured color gradients decrease by \sim 0.3 dex. The Dutton et al. (2011) model did not, however, account for the effects of dust or mergers. Both dust and mergers can affect the strength of color gradients in galaxies, and their inclusion in the Dutton et al. (2011) models would likely change how their simulated color gradients evolve. There are no studies which examine color gradient strength or evolution in modern high-resolution cosmological simulations. Such studies would provide an invaluable comparison to our recent observations, and allow us to more fully contextualize our findings in this paper.

Such a comparison of simulated and observed half-mass radii and color gradients—while necessary—will also be difficult. There are a host of choices to make when analyzing simulations that complicate a direct comparison with observations. Aperture effects can bias galaxy sizes by ~ 0.1 dex, and varying the viewing angle can change the inferred half-light size by $\sim 0.1-0.2$ dex (Price et al. 2017). Even the total stellar



Figure 4. Half-light radius (open gray points) and half-mass radius (filled black points) of star-forming galaxies at $10^{10.5} M_{\odot}$ as a function of lookback time. Half-mass radii evolve much less rapidly than half-light radii.

mass of the galaxy—and thus its location in the mass-size diagram—can change based on how far out the mass profile is integrated (causing variations of 0.1–0.2 dex; Genel et al. 2018) and/or differences in the stellar mass loss prescription used by the simulation and by the stellar population synthesis modeling of the observations (e.g., Price et al. 2017). Selection effects may also play a role: our observations compare the sizes of star-forming and quiescent galaxies at fixed mass, but if these populations evolve differently in the simulations (e.g., if galaxies quench at a different rate), then the galaxy populations will differ between the observations and simulations. To perform a fair comparison between observations and simulations, it is thus necessary to analyze mock observations of the simulations using the *same techniques* that are used for the real observations (see Price et al. 2017).

Finally, we note that measuring color gradients and halfmass radii from observed data is difficult; we refer the reader to Suess et al. (2019) for a full discussion of the sources of possible biases in our measurements. In particular, it is difficult to account for the most highly dust-obscured star formation with our methods. Measurements at longer wavelengths (with ALMA, e.g., Barro et al. 2016), are crucial to understand the mass profiles of such obscured systems.

6. Summary

In this Letter, we extended the Suess et al. (2019) analysis of color gradients and half-mass radii of both star-forming and quiescent galaxies to $z \sim 0$. This data set, together with our previous results, represents the largest collection of galaxy half-mass radii at z > 0 in the literature. This large sample of half-mass radii, calculated in a uniform way across a wide range of redshifts and stellar masses, allows us to conduct a detailed

examination of how the half-mass sizes of galaxies grow over cosmic time.

We find that color gradients in both star-forming and quiescent galaxies evolve between z = 2.5 and $z \sim 0$. When taking these color gradients into account, the sizes of both star-forming and quiescent galaxies grow much less rapidly than previously found. For quiescent galaxies, the evolution of half-mass radii is fully consistent with the expected growth due to minor mergers *alone* (Figure 3) based on the observed merger rates of Newman et al. (2012) and assuming a relatively fast merger timescale of 1 Gyr. A slower merger timescale would allow additional room for progenitor bias to contribute to the growth of quiescent galaxies. For star-forming galaxies, the evolution of half-mass radii is much slower than predicted by cosmological simulations and semianalytic models, and raises questions as to the physical mechanisms responsible for this slow size growth.

Further work is required to reconcile these new observational results with the apparent consensus in the literature. For quiescent galaxies, the magnitude of growth due to progenitor bias is still not fully understood; this may be addressed by detailed examinations of the half-mass radii of the smallest galaxies over cosmic time (as in Carollo et al. 2013; Poggianti et al. 2013). The slow size evolution of star-forming galaxies is more challenging to address, as it is in tension with available theoretical predictions. Additional work to understand the effects of feedback and mergers on half-mass radii and color gradients is required to address this discrepancy. Finally, studies that directly compare half-mass and half-light radii in cosmological simulations in a consistent manner as the observations (e.g., Price et al. 2017) are essential to understand the origins and impacts of our observed evolving color gradients.

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